Supplemental Material

Visual Parameter Space Analysis: A Conceptual Framework

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Abstract

This supplemental material provides (1) additional methodological details of the conducted literature analysis and (2) a list of all 112 papers that we considered for this analysis.

1 Identification of Relevant Literature

The selection process of papers to be included in our work "Visual Parameter Space Analysis: A Conceptual Framework" was based on a broad initial literature study. We started off with a search on parameter space analysis papers in core relevant visualization conferences and journals:

- IEEE Transactions on Visualization and Computer Graphics (TVCG, including InfoVis and SciVis special issues)
- IEEE Conference on Visual Analytics Science and Technology (VAST)
- Computer Graphics Forum (including EuroVis special issue)
- IEEE Pacific Visualization Symposium (PacificVis)
- IEEE Computer Graphics and Applications
- Computers and Graphics
- The Visual Computer
- MICCAI
- VMV

Then, we also had an eye on other related areas in a second step, e.g.:

- IEEE Transactions on Pattern Analysis and Machine Intelligence
- Computational Statistics
- Computer Vision
- Machine Learning
- Machine Graphics and Vision
- ACM SIGGRAPH
- Eurographics Symposium on Computer Animation
- ACM SIGMOD International Conference on Management of Data
- ACM Symposium on User interface software and technology (UIST)

Based on the references given in those selected papers of visualization as well as the related areas, we finally also included related work from more application-driven angles:

- Journal of Geophysical Research: Oceans
- Frontiers in Neuroinformatics
- Psychological Review
- Journal of Applied Mechanics Technometrics
- Journal of Marine Research
- Journal of the Royal Statistical Society

We broadly surveyed titles and abstracts of papers published in these venues, guided by our own previous experience and by following promising references. Our literature list, which we generated from this process, contained in total 112 papers. In a second step, we classified these papers as "core-relevant" (21 papers), "related" (37), "slightly related" (27), and "marginally related" (27) with respect to our focus on and understanding of visual parameter space analysis. Note, that when we started the literature identification process, the scope of

our work was broader. In particular, our initial focus also included work related to more general *uncertainty visualization*. After we decided to narrow down the scope more specifically to visual parameter space analysis, papers that address aspects of uncertainty only were classified as "marginally related".

2 Analysis Process

The 21 core-relevant papers were analyzed in two main phases, a "training" and a "validation" phase.

Phase 1 (training): 14 of the "core-relevant" papers have undergone a detailed open coding process to figure out which tasks are of interest, which goals and objectives the papers are sharing, and which strategies have been applied to support these tasks and goals. We used this analysis to inform and refine an initial version of the framework that we developed based on our own experience working in visual parameter space analysis. This open coding process in turn was based on three rounds of iteration:

Phase 1.1: In the first round, 10 of the 14 papers were coded by the first and the second author [1, 3, 7, 12, 14, 16, 17, 18, 19, 21]. We very broadly coded all aspects that might be potentially of interest for our framework. We also coded another paper that turned out not to be core-relevant to our analysis [83], due to its focus on output visualization. The results were analyzed using affinity diagramming and then discussed amongst all authors.

Phase 1.2: The other 4 papers were coded by all authors [8, 13, 15, 20]. A fifth paper that was coded in this phase turned out to be not core-relevant [35]. Discussions of these papers resulted in further refinements of the framework, agreeing on a shared understanding among all authors, as well as the finalization of concrete inclusion/exclusion criteria as described below.

Phase 1.3: All 14 papers, were re-visited in order to adapt their classification according to the framework changes that have been undertaken. To do so, each paper was re-coded by pairs of two authors and then discussed among them to agree on a final classification.

Phase 2 (validation): We coded the remaining 7 of the 21 core-relevant papers to validate the final version of our framework [2, 4, 5, 6, 9, 10, 11]. In this phase, we classified the papers without adapting the framework anymore. Again, each paper was separately analyzed by two authors. Subsequently, the results were discussed and merged together to a final classification.

Naturally, there was some overlay between literature identification (Section 1) and analysis (this section).

3 Inclusion/Exclusion Criteria

In phase 1.2., we specified three inclusion/exclusion criteria. We used these criteria to reiterate and refine our set of "core-relevant" papers.

- 1. Criterion—Match our definition of parameter space analysis. All core-relevant papers should follow our definition of parameter space analysis: "Parameter space analysis (PSA) is the systematic variation of model input parameters, generating outputs for each combination of parameters, and investigating the relation between parameter settings and corresponding outputs." (Section 1.1 in the paper). This definition was based on the initial analysis of 10 papers (phase 1.1) and our own previous experience.
- Following this definition had several implications. First, a simulation or an algorithmic model needs to exist in order to sample and analyze the parameter space. We therefore excluded papers that discuss solutions for purely measured data. For measured data, sampling is of no primary concern to the analysis chain. Second, we excluded papers that discuss visual representations for model outputs only, without a dedicated focus on the relation between inputs and outputs. Third, we also primarily focused on model validation and usage rather than on model building, where a full model does not exist yet.
- 2. Criterion—Focus on visual approaches. Our focus was on papers using interactive visualization techniques for parameter space analysis. We specifically excluded purely automatic solutions (e.g., machine learning approaches).
- **3.** Criterion—Concrete applications. Finally, to allow us to properly evaluate tasks, we put a strong focus on the presentation of concrete applications. In particular, we sought for papers that demonstrated the proposed solutions with specific use cases or application scenarios. We excluded several papers that did not provide enough application details to meaningfully code analysis tasks. For papers with a substantial similarity in the presented application scenarios, we selected one representative for our analysis of core-relevant papers.

4 Analysis of Remaining Papers

The remaining papers were analyzed in another step. For the "related" and "slightly related" categories, we extracted aspects of interest on a case-by-case basis in order to suitably address them in the paper. The category of "marginally related" papers has not been actively considered any further in this work. We include the full literature list of all 112 papers below.

5 List of All 112 Papers

Core-relevant Papers

- S. Afzal, R. Maciejewski, and D.S. Ebert. Visual analytics decision support environment for epidemic modeling and response evaluation. In *IEEE Con*ference on Visual Analytics Science and Technology (VAST) 2011, pages 191–200, 2011.
- [2] A. Amirkhanov, C. Heinzl, M. Reiter, and M. E. Gröller. Visual optimality and stability analysis of 3DCT scan positions. *IEEE Transactions on Visualization and Computer Graphics*, 16(6):1477–1487, Oct 2010.
- [3] W. Berger, H. Piringer, P. Filzmoser, and E. Gröller. Uncertainty-aware exploration of continuous parameter spaces using multivariate prediction. Computer Graphics Forum (Eurographics / IEEE Symposium on Visualization 2011 (Euro Vis 2011)), 30(3):911–920, 2011.
- [4] S. Bergner, M. Sedlmair, T. Möller, S. Nabi Abdolyousefi, and A. Saad. Paraglide: Interactive parameter space partitioning for computer simulations. *IEEE Transactions on Visualization and Computer Graphics*, 19(9):1499–1512, Sept 2013.
- [5] M. Booshehrian, T. Möller, R. M. Peterman, and T. Munzner. Vismon: Facilitating analysis of trade-offs, uncertainty, and sensitivity in fisheries management decision making. Computer Graphics Forum (Eurographics / IEEE-VGTC Symposium on Visualization (EuroVis 2012)), 31(3):1235– 1244, Jun 2012.
- [6] R. Brecheisen, A. Vilanova, B. Platel, and B. ter Haar Romeny. Parameter sensitivity visualization for DTI fiber tracking. *IEEE Transactions on Visualization and Computer Graphics*, 15(6):1441–1448, 2009.
- [7] S. Bruckner and T. Möller. Result-driven exploration of simulation parameter spaces for visual effects design. *IEEE Transactions on Visualization and Computer Graphics*, 16(6):1467–1475, October 2010.
- [8] D. Coffey, Chi-Lun Lin, A.G. Erdman, and D.F. Keefe. Design by dragging: An interface for creative forward and inverse design with simulation ensembles. *IEEE Transactions on Visualization and Computer Graphics*, 19(12):2783–2791, 2013.
- [9] Z. Guo, M. O. Ward, and E. A. Rundensteiner. Model space visualization for multivariate linear trend discovery. In *IEEE Symposium on Visual Analytics Science and Technology (VAST)*, 2009, pages 75–82, Oct 2009.
- [10] Z. Konyha, K. Matkovic, D. Gracanin, M. Jelovic, and H. Hauser. Interactive visual analysis of families of function graphs. *IEEE Transactions on Visualization and Computer Graphics*, 12(6):1373–1385, November 2006.

- [11] M. Luboschik, S. Rybacki, F. Haack, and H.J. Schulz. Supporting the integrated visual analysis of input parameters and simulation trajectories. *Computers & Graphics*, 39:37–47, 2014.
- [12] J. Marks, B. Andalman, P. A. Beardsley, W. Freeman, S. Gibson, J. Hodgins, T. Kang, B. Mirtich, H. Pfister, W. Ruml, K. Ryall, J. Seims, and S. Shieber. Design galleries: a general approach to setting parameters for computer graphics and animation. In ACM Computer Graphics (SIG-GRAPH '97 Proceedings), SIGGRAPH '97, pages 389–400, New York, NY, USA, 1997. ACM Press/Addison-Wesley Publishing Co.
- [13] K. Matkovic, D. Gracanin, M. Jelovic, and H. Hauser. Interactive visual steering - rapid visual prototyping of a common rail injection system. *IEEE Transactions on Visualization and Computer Graphics*, 14(6):1699–1706, November 2008.
- [14] K. Matkovic, D. Gracanin, B. Klarin, and H. Hauser. Interactive visual analysis of complex scientific data as families of data surfaces. *IEEE Trans*actions on Visualization and Computer Graphics, 15(6):1351–1358, 2009.
- [15] H. Piringer, W. Berger, and J. Krasser. HyperMoVal: interactive visual validation of regression models for real-time simulation. *Computer Graphics Forum, Eurographics / IEEE-VGTC Symposium on Visualization (EuroVis 2010)*, 29(3):983–992, 2010.
- [16] K. Potter, A. Wilson, P.-T. Bremer, D. Williams, C. Doutriaux, V. Pascucci, and C.R. Johnson. Ensemble-Vis: A framework for the statistical visualization of ensemble data. In *Proceedings of the 2009 IEEE International Conference on Data Mining Workshops*, pages 233–240, 2009.
- [17] A. J. Pretorius, M.-A. P. Bray, A. E. Carpenter, and R. A. Ruddle. Visualization of parameter space for image analysis. *IEEE Transactions on Visualization and Computer Graphics*, 17(12):2402–2411, 2011.
- [18] B. Spence, L. Tweedie, H. Dawkes, and Hua Su. Visualization for functional design. In *Proceedings of the 1995 IEEE Symposium on Information Vi*sualization, INFOVIS '95, pages 4–10, Washington, DC, USA, 1995. IEEE Computer Society.
- [19] T. Torsney-Weir, A. Saad, T. Möller, H.C. Hege, B. Weber, and J.M. Verbavatz. Tuner: Principled parameter finding for image segmentation algorithms using visual response surface exploration. *IEEE Transactions on Visualization and Computer Graphics*, 17(12):1892–1901, 2011.
- [20] A. Unger, S. Schulte, V. Klemann, and D. Dransch. A visual analysis concept for the validation of geoscientific simulation models. *IEEE Trans*actions on Visualization and Computer Graphics, 18(12):2216–2225, 2012.

[21] J. Waser, R. Fuchs, H. Ribicic, B. Schindler, G. Blöschl, and E. Gröller. World lines. *IEEE Transactions on Visualization and Computer Graphics*, 16(6):1458–1467, 2010.

Related Papers

- [22] Z. Ahmed and C. Weaver. An adaptive parameter space-filling algorithm for highly interactive cluster exploration. In *IEEE Conference on Visual Analytics Science and Technology (VAST) 2012*, pages 13–22, 2012.
- [23] C. L. Bajaj, V. Pascucci, and D. R. Schikore. The contour spectrum. In *Visualization '97.*, *Proceedings*, pages 167–173, 1997.
- [24] M. J. Bayarri, J. O. Berger, E. S. Calder, K. Dalbey, S. Lunagomez, A. K. Patra, E. B. Pitman, E. T. Spiller, and R. L. Wolpert. Using statistical and computer models to quantify volcanic hazards. *Technometrics*, 51(4):402–413, 2009.
- [25] M. Bögl, W. Aigner, P. Filzmoser, T. Lammarsch, S. Miksch, and A Rind. Visual analytics for model selection in time series analysis. *IEEE Transactions on Visualization and Computer Graphics*, 19(12):2237–2246, Dec 2013.
- [26] U. D. Bordoloi and Han-Wei Shen. View selection for volume rendering. In *IEEE Visualization*, 2005 (VIS'05), pages 487–494, 2005.
- [27] I. Bowman, Joshi S.H., and J.D. Van Horn. Visual systems for interactive exploration and mining of large-scale neuroimaging data archives. *Frontiers in Neuroinformatics*, 6:11, 2012.
- [28] S. Bruckner and T. Möller. Isosurface similarity maps. Computer Graphics Forum, Eurographics / IEEE-VGTC Symposium on Visualization (EuroVis 2010), 29(3):773–782, June 2010.
- [29] Y.-H. Chan, C. Correa, and K.-L. Ma. Flow-based scatterplots for sensitivity analysis. In *IEEE Symposium on Visual Analytics Science and Technology (VAST) 2010*, pages 43–50, 2010.
- [30] H. Doleisch. SimVis: Interactive visual analysis of large and time-dependent 3d simulation data. In Simulation Conference, 2007 Winter, pages 712–720, 2007.
- [31] N. Ferreira, L. Lins, D. Fink, S. Kelling, C. Wood, J. Freire, and C. Silva. BirdVis: Visualizing and understanding bird populations. *IEEE Transactions on Visualization and Computer Graphics*, 17(12):2374–2383, 2011.
- [32] S. Gerber, P. Bremer, V. Pascucci, and R. Whitaker. Visual exploration of high dimensional scalar functions. *IEEE Transactions on Visualization and Computer Graphics*, 16(6):1271–1280, 2010.

- [33] W. A. Gough and W. J. Welch. Parameter space exploration of an ocean general circulation model using an isopycnal mixing parameterization. *Journal of Marine Research*, 52(5):773–796, 1994.
- [34] R. B. Gramacy, H. K. H. Lee, and W. G. Macready. Parameter space exploration with Gaussian process trees. In *Proceedings of the 21st International Conference on Machine Learning*, ICML'04, pages 353âĂŞ-360, New York, NY, USA, 2004. ACM.
- [35] Z. Guo, M. O. Ward, E. A. Rundensteiner, and C. Ruiz. Pointwise local pattern exploration for sensitivity analysis. In *IEEE Conference on Visual Analytics Science and Technology (VAST) 2011*, pages 131–140, Oct 2011.
- [36] M. Hadwiger, L. Fritz, C. Rezk-Salama, T. Höllt, G. Geier, and T. Pabel. Interactive volume exploration for feature detection and quantification in industrial CT data. *IEEE Transactions on Visualization and Computer Graphics*, 14(6):1507–1514, November 2008.
- [37] M. Haidacher, S. Bruckner, and M. E. Gröller. Volume analysis using multimodal surface similarity. *IEEE Transactions on Visualization and Computer Graphics*, 17(12):1969–1978, October 2011.
- [38] M. Haidacher, D. Patel, S. Bruckner, A. Kanitsar, and M.E. Gröller. Volume visualization based on statistical transfer-function spaces. In *Proceedings of the IEEE Pacific Visualization 2010*, pages 17–24, March 2010.
- [39] L. Huettenberger, C. Heine, H. Carr, G. Scheuermann, and C. Garth. Towards multifield scalar topology based on Pareto optimality. *Computer Graphics Forum*, 32(3):341–350, 2013.
- [40] D. R. Jones, M. Schonlau, and W. J. Welch. Efficient global optimization of expensive black-box functions. *Journal of Global Optimization*, 13(4):455–492, December 1998.
- [41] X. Lin, A. Mukherji, E. A. Rundensteiner, C. Ruiz, and M. O. Ward. PARAS: Parameter space framework for online association mining. In *Proceedings of the VLDB Endowment*, volume 6, 2013.
- [42] H. Loeffelmann, E. Gröller, R. Wegenkittl, and W. Purgathofer. Classifying the visualization of analytically specified dynamical systems. *Machine Graphics & Vision*, 5(4):533–550, 1996.
- [43] R. M. Martins, D. B. Coimbra, R. Minghim, and A.C. Telea. Visual analysis of dimensionality reduction quality for parameterized projections. *Computers & Graphics*, 41:26–42, 2014.
- [44] K. Matkovic, D. Gracanin, M. Jelovic, A. Ammer, A. Lez, and H. Hauser. Interactive visual analysis of multiple simulation runs using the simulation model view: Understanding and tuning of an electronic unit injector. *IEEE Transactions on Visualization and Computer Graphics*, 16(6):1449–1457, 2010.

- [45] K. Matkovic, M. Jelovic, J. Juric, Z. Konyha, and D. Gracanin. Interactive visual analysis and exploration of injection systems simulations. In *IEEE Visualization 2005*, pages 391–398, 2005.
- [46] M. Monks, B.M. Oh, and J. Dorsey. Audioptimization: Goal-based acoustic design. *IEEE Computer Graphics and Applications*, 20(3):76–90, 2000.
- [47] T. Mühlbacher and H. Piringer. A partition-based framework for building and validating regression models. *IEEE Transactions on Visualization and Computer Graphics*, 19(12):1962–1971, 2013.
- [48] T. Nocke, M. Flechsig, and U. Bohm. Visual exploration and evaluation of climate-related simulation data. In *Simulation Conference*, 2007 Winter, pages 703–711, 2007.
- [49] L. Padua, H. Schulze, K. Matkovic, and C. Delrieux. Interactive exploration of parameter space in data mining: Comprehending the predictive quality of large decision tree collections. *Computers & Graphics*, 41:99–113, 2014.
- [50] H. Piringer, S. Pajer, W. Berger, and H. Teichmann. Comparative visual analysis of 2D function ensembles. Computer Graphics Forum, 31(3pt3):1195–1204, Jun 2012.
- [51] K. Potter, A. Wilson, P.-T. Bremer, D. Williams, C. Doutriaux, V. Pascucci, and C.R. Johnson. Visualization of uncertainty and ensemble data: Exploration of climate modeling and weather forecast data with integrated ViSUS-CDAT systems. In *Proceedings of SciDAC 2009*, volume 180 of *Journal of Physics: Conference Series*, page (published online), 2009.
- [52] C. A. Shaffer, D. L. Knill, and L. T. Watson. Visualization for multiparameter aircraft designs. In *Visualization '98. Proceedings*, pages 491–494, 1998.
- [53] R. C. Smith, R. Pawlicki, I. R. Kokai, J. Finger, and T. Vetter. Navigating in a shape space of registered models. *IEEE Transactions on Visualization and Computer Graphics*, 13(6):1552–1559, 2007.
- [54] L. Tweedie and R. Spence. The prosection matrix: A tool to support the interactive exploration of statistical models and data. *Computational Statistics*, 13(1):65–76, 1998.
- [55] L. Tweedie, R. Spence, H. Dawkes, and Hus Su. Externalising abstract mathematical models. In *Proceedings of the SIGCHI Conference on Human Factors in Computing Systems*, pages 406–412. ACM, 1996.
- [56] J. J. van Wijk and R. van Liere. HyperSlice: Visualization of scalar functions of many variables. In *Proceedings IEEE Visualization âĂŹ93*, VIS '93, pages 119–125, Washington, DC, USA, 1993. IEEE Computer Society.

- [57] A. T. Wilson and K. C. Potter. Toward visual analysis of ensemble data sets. In *Proceedings of the 2009 Workshop on Ultrascale Visualization*, UltraVis '09, pages 48–53, New York, NY, USA, 2009. ACM.
- [58] H. Wright, K. Brodlie, and T. David. Navigating high-dimensional spaces to support design steering. In *Visualization 2000. Proceedings*, pages 291– 296. IEEE, 2000.

Slightly Related Papers

- [59] S. Bachthaler and D. Weiskopf. Continuous scatterplots. *IEEE Transactions on Visualization and Computer Graphics*, 14(6):1428–1435, 2008.
- [60] S. Bhagavatula, P. Rheingans, and M. desJardins. Discovering high-level parameters for visualization design. In *Eurographics-IEEE VGTC Symposium on Visualization*, pages 255–262. Eurographics Association, 2005.
- [61] V. Bhatt and J. Koechling. Partitioning the parameter space according to different behaviors during three-dimensional impacts. *Journal of Applied Mechanics*, 62(3):740–746, 1995.
- [62] G.E.P. Box and K.B. Wilson. On the experimental attainment of optimum conditions. *Journal of the Royal Statistical Society. Series B (Methodological)*, 13(1):1–45, 1951.
- [63] E. Brochu, T. Brochu, and N. de Freitas. A Bayesian interactive optimization approach to procedural animation design. In *Proceedings of the 2010 ACM SIGGRAPH/Eurographics Symposium on Computer Animation*, SCA '10, pages 103–112, Aire-la-Ville, Switzerland, Switzerland, 2010. Eurographics Association.
- [64] S. P. Callahan, J. Freire, E. Santos, C. E. Scheidegger, C. T. Silva, and H. T. Vo. VisTrails: Visualization meets data management. In *Proceedings* of the 2006 ACM SIGMOD International Conference on Management of Data, pages 745–747. ACM, 2006.
- [65] W. L. Chapman, W. J. Welch, K. P. Bowman, J. Sacks, and J. E. Walsh. Arctic sea ice variability: Model sensitivities and a multidecadal simulation. *Journal of Geophysical Research: Oceans* (1978–2012), 99(C1):919–935, 1994.
- [66] C. Dick, R. Burgkart, and R. Westermann. Distance visualization for interactive 3D implant planning. *IEEE Transactions on Visualization and Computer Graphics*, 17(12):2173–2182, 2011.
- [67] L. Fritz, M. Hadwiger, G. Geier, G. Pittino, and E. Gröller. A visual approach to efficient analysis and quantification of ductile iron and reinforced sprayed concrete. *IEEE Transactions on Visualization and Com*puter Graphics, 15(6):1343–1350, 2009.

- [68] S. Gratzl, A. Lex, N. Gehlenborg, H.P. Pfister, and M. Streit. LineUp: Visual analysis of multi-attribute rankings. *IEEE Transactions on Visual-ization and Computer Graphics*, 19(12):2277–2286, 2013.
- [69] E. Gröller. Application of visualization techniques to complex and chaotic dynamical systems. In *Proceedings of the 5th Eurographics Workshop on Visualization in Scientific Computing*, pages Workshop in Scientific Computing, May 1994.
- [70] S. Gumhold. Maximum entropy light source placement. In *Visualization*, 2002. VIS 2002. IEEE, pages 275–282, 2002.
- [71] J. Heinrich and D. Weiskopf. Continuous parallel coordinates. *IEEE Transactions on Visualization and Computer Graphics*, 15(6):1531–1538, 2009.
- [72] T. J. Jankun-Kelly, K.-L. Ma, and M. Gertz. A model and framework for visualization exploration. *IEEE Transactions on Visualization and Com*puter Graphics, 13(2):357–369, 2007.
- [73] S. Jayaraman and C. North. A radial focus+context visualization for multidimensional functions. In *Proceedings Visualization '02*, VIS '02, pages 443–450, Washington, DC, USA, 2002. IEEE Computer Society.
- [74] J. Kronander, J. Unger, T. Möller, and A. Ynnerman. Estimation and modeling of actual numerical errors in volume rendering. *Computer Graphics Forum, Eurographics / IEEE-VGTC Symposium on Visualization (Euro-Vis 2010)*, 29(3):893–902, June 2010.
- [75] K.-L. Ma. Image graphs-a novel approach to visual data exploration. In *Proceedings Visualization '99*, pages 81–88, 1999.
- [76] C. McIntosh and G. Hamarneh. Optimal weights for convex functionals in medical image segmentation. In Advances in Visual Computing, pages 1079–1088. Springer, 2009.
- [77] M. A. Pitt, W. Kim, D. J. Navarro, and J. I. Myung. Global model analysis by parameter space partitioning. *Psychological Review*, 113(1):57, 2006.
- [78] K. Pöthkow, B. Weber, and H. C. Hege. Probabilistic Marching Cubes. Computer Graphics Forum (Euro Vis 2011), 30(3):931–940, 2011.
- [79] K. Potter, J. Kniss, R. Riesenfeld, and C.R. Johnson. Visualizing summary statistics and uncertainty. In *Computer Graphics Forum (Proceedings of EuroVis 2010)*, volume 29, pages 823–831, 2010.
- [80] A. Saad, G. Hamarneh, and T. Möller. Exploration and visualization of segmentation uncertainty using shape and appearance prior information. *IEEE Transactions on Visualization and Computer Graphics*, 16(6):1366– 1375, 2010.

- [81] A. Saad, T. Möller, and G. Hamarneh. ProbExplorer: Uncertainty-guided exploration and editing of probabilistic medical image segmentation. Computer Graphics Forum, Eurographics / IEEE-VGTC Symposium on Visualization (Euro Vis 2010), 29(3):1113-1120, June 2010 2010.
- [82] T. W. Simpson, V. V. Toropov, V. Balabanov, and F. A. C. Viana. Design and analysis of computer experiments in multidisciplinary design optimization: A review of how far we have come or not. In 12th AIAAISSMO Multidisciplinary Analysis and Optimization Conference, pages 10–12, 2008.
- [83] A. Unger and H. Schumann. Visual support for the understanding of simulation processes. In *Visualization Symposium*, 2009. Pacific Vis '09. IEEE Pacific, pages 57–64, 2009.
- [84] I. Viola, M. Feixas, M. Sbert, and M.E. Gröller. Importance-driven focus of attention. *IEEE Transactions on Visualization and Computer Graphics*, 12(5):933–940, 2006.
- [85] M. O. Ward. XmdvTool: Integrating multiple methods for visualizing multivariate data. In *Proceedings Visualization '94*, pages 326–333, 1994.

Marginally Related Papers

- [86] H. Bhatia, S. Jadhav, P.-T. Bremer, G. Chen, J.A. Levine, L.G. Nonato, and V. Pascucci. Edge maps: Representing flow with bounded error. In Proceedings of IEEE Pacific Visualization Symposium 2011, pages 75–82, March 2011.
- [87] Y. Boykov, O. Veksler, and R. Zabih. Fast approximate energy minimization via graph cuts. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 23(11):1222–1239, 2001.
- [88] S. Djurcilov, K. Kim, P. Lermusiaux, and A. Pang. Visualizing scalar volumetric data with uncertainty. *Computers & Graphics*, 26:239–248, 2002.
- [89] S. K. Feiner and C. Beshers. Worlds within worlds: metaphors for exploring n-dimensional virtual worlds. In *Proceedings of the 3rd annual ACM Symposium on User Interface Software and technology*, UIST '90, pages 76–83, New York, NY, USA, 1990. ACM.
- [90] L. Grady. Random walks for image segmentation. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 28(11):1768–1783, 2006.
- [91] C. Heinzl, J. Kastner, T. Möller, and M. E. Gröller. Statistical analysis of multi-material components using dual energy CT. In VMV 2008, Vision, Modeling and Visualization, pages 179–188, 2008.
- [92] A. Inselberg and B. Dimsdale. Parallel coordinates: a tool for visualizing multi-dimensional geometry. In *Proceedings Visualization '90*, pages 361–378, 1990.

- [93] C.Y. Ip, A. Varshney, and J. Jaja. Hierarchical exploration of volumes using multilevel segmentation of the intensity-gradient histograms. *IEEE Transactions on Visualization and Computer Graphics*, 18(12):2355–2363, 2012.
- [94] C. R. Johnson. Top scientific visualization research problems. *IEEE Computer Graphics and Applications*, 24(4):13–17, July/August 2004.
- [95] C. R. Johnson and A. R. Sanderson. A next step: Visualizing errors and uncertainty. *IEEE Computer Graphics and Applications*, 23(5):6–10, 2003.
- [96] O. van Kaick, A. Tagliasacchi, O. Sidi, H. Zhang, D. Cohen-Or, L. Wolf, and G. Hamarneh. Prior knowledge for part correspondence. Computer Graphics Forum (Proceedings of Eurographics 2011), 30:553–562, 01/2011 2011.
- [97] J. M. Kniss, R. Van Uitert, A. Stephens, G.-S. Li, T. Tasdizen, and C. Hansen. Statistically quantitative volume visualization. In *Visualization*, 2005. VIS 05. IEEE, pages 287–294, oct 2005.
- [98] S. Kumar and M. Hebert. Discriminative random fields: a discriminative framework for contextual interaction in classification. In *Computer Vision*, 2003. Proceedings. Ninth IEEE International Conference on, pages 1150–1157 vol.2, 2003.
- [99] S. K. Lodha, A. Pang, R. E. Sheehan, and C. M. Wittenbrink. Uflow: visualizing uncertainty in fluid flow. In *Visualization '96. Proceedings.*, pages 249–254, nov 1996.
- [100] K. Mühler, M. Neugebauer, C. Tietjen, and B. Preim. Viewpoint selection for intervention planning. In *Proceedings of the 9th Joint Eurographics* / *IEEE VGTC Conference on Visualization*, EuroVis'07, pages 267–274, Aire-la-Ville, Switzerland, Switzerland, 2007. Eurographics Association.
- [101] C. McIntosh and G. Hamarneh. Is a single energy functional sufficient? Adaptive energy functionals and automatic initialization. In *Proceedings of the 10th International Conference on Medical Image Computing and Computer-assisted Intervention*, MICCAI'07, pages 503–510, Berlin, Heidelberg, 2007. Springer-Verlag.
- [102] M. Otto, T. Germer, H.C. Hege, and H. Theisel. Uncertain 2D vector field topology. *Computer Graphics Forum (Proceedings of Eurographics 2010)*, 29(2):347–356, 2010.
- [103] A. Pang, C. Wittenbrink, and S. Lodha. Approaches to uncertainty visualization. *The Visual Computer*, 13:370–390, 1997.
- [104] T. Pfaffelmoser, M. Reitinger, and R. Westermann. Visualizing the positional and geometrical variability of isosurfaces in uncertain scalar fields. In *Proceedings of the 13th Eurographics / IEEE VGTC Conference on Visualization*, EuroVis'11, pages 951–960, 2011.

- [105] K. Pöthkow and H. C. Hege. Positional uncertainty of isocontours: Condition analysis and probabilistic measures. *IEEE Transactions on Visualization and Computer Graphics*, 17(10):1393–1406, 2011.
- [106] K. Potter, J. Krüger, and C. Johnson. Towards the visualization of multidimensional stochastic distribution data. In *Proceedings of The Interna*tional Conference on Computer Graphics and Visualization (IADIS), 2008.
- [107] C. E. Scheidegger, H. T. Vo, D. Koop, J. Freire, and C. T. Silva. Querying and creating visualizations by analogy. *IEEE Transactions on Visualization* and Computer Graphics, 13(6):1560–1567, 2007.
- [108] P. Sereda, A.V. Bartroli, I.W.O. Serlie, and F.A. Gerritsen. Visualization of boundaries in volumetric data sets using LH histograms. *IEEE Trans*actions on Visualization and Computer Graphics, 12(2):208–218, 2006.
- [109] M. Szummer, P. Kohli, and D. Hoiem. Learning CRFs using graph cuts. In *Computer Vision (ECCV '08)*, pages 582–595. Springer, 2008.
- [110] S. Takahashi, I. Fujishiro, Y. Takeshima, and T. Nishita. A feature-driven approach to locating optimal viewpoints for volume visualization. In *Visualization*, 2005. VIS 05. IEEE, pages 495–502, 2005.
- [111] G. H. Weber, P.-T. Bremer, and V. Pascucci. Topological landscapes: A terrain metaphor for scientific data. *IEEE Transactions on Visualization and Computer Graphics*, 13(6):1416–1423, 2007.
- [112] C. M. Wittenbrink, A. T. Pang, and S. K. Lodha. Glyphs for visualizing uncertainty in vector fields. *IEEE Transactions on Visualization and Computer Graphics*, 2(3):266–279, September 1996.